

# MODERNIZATION OF STATISTICAL PROCEDURES FOR WATER SUPPLY FORECASTING

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## ABSTRACT

The promise of conceptual watershed models and extended streamflow prediction all but terminated statistical water supply forecasting technique development by the National Weather Service in the early 1980's. Statistical procedures have, however, remained the dominant technique and will have a role when conceptual watershed models become dominant in use. Recognizing this, the Colorado Basin River Forecast Center (CBRFC) modernized its' statistical water supply forecasting system to take advantage of current technology and resources.

The system described includes a database, calibration, and operational component. The system was designed to make calibration and operational use fast, simple, and informative. System flexibility allows the hydrologic developer to structure procedures as desired using any information deemed appropriate. As such, weather indices and long range weather forecasts can be used. Application of the system significantly improved the quality of water supply forecasts issued by the CBRFC during water year 1993.

## INTRODUCTION

Water resources management is critical in the Western U.S. Water supply forecasts provided by the National Weather Service (NWS) in cooperation with the Soil Conservation Service (SCS) and other cooperators allow resource managers and agricultural interests to scale operations to the available water supply. This service provides significant economic, environmental, and social benefits to the region. Improvements in the quality of forecasts can be directly translated into economic benefits (Castruccio et al., 1981).

As the population of the West has grown, the demands on water resources have, in many cases, exceeded supply. Water is perhaps the principal natural resource that governs the development of the Western U.S. As such, the need for accurate and timely water resource forecasts is important today and will become increasingly important in the future.

Water supply forecasts have been made in the West for nearly 60 years. Early efforts were simple and limited in scale. Starting in the 1950's, the NWS began to develop and issue seasonal volume forecasts. Techniques developed at that time included simple linear regression of lumped indices or multiple linear regression. Each NWS River Forecast Center (RFC) developed a similar yet unique method of calibrating and operationally evaluating water supply procedures. Computer and data resources available in the 1960's and early 1970's limited the development of optimal procedures.

With the development of conceptual (physically based) models and Extended Streamflow Prediction (ESP) within the NWS River Forecast System (NWSRFS) (Twedt et al., 1978; Curtis and Schakke, 1979; Day, 1985), the place of statistically based water supply procedures appeared limited. Clearly a conceptual model is more temporally flexible and more accurately can predict extreme events. Additionally it can provide a variety of hydrologic information about a specific basin. Unfortunately, the vision of this ultimate forecasting system sidelined the natural development and maintenance of the statistically based models. In time, the statistical forecasting system in use became outdated.

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Conceptual model calibration and operational application of ESP has not been quick. Batch calibration and poor data resources make the calibration process awkward, time consuming, and non-optimal. In time, the calibration of conceptual models within NWSRFS will be interactive and near-optimal. Currently, the CBRFC and other RFCs use statistical procedures as the principal water supply forecasting tool with ESP as a complementary and time-distributing tool. Additionally, ESP, when calibrated and available, is used to provide intermediate duration (i.e. 2 week) volume and peak forecasts. The CBRFC recognizes that conceptual models represent the future of water resources forecasting and hence the dominant and supportive roles of statistical and conceptual models will eventually be reversed. In the meantime, it is imperative that the NWS provide the best possible guidance to its' users as the move is made towards this new environment.

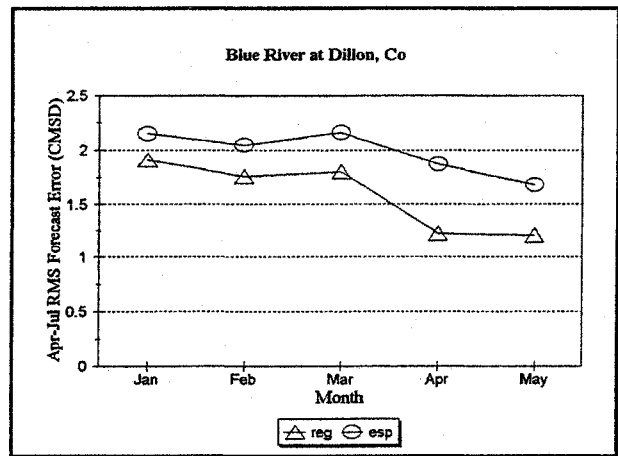


Figure 1. Comparison of regression and ESP based RMS forecast errors for the April-July period (1961-1988), Blue River at Dillon, CO.

Given that conceptual models offer greater flexibility and improved performance at the extremes, do statistical models have a place in a modernized forecasting system? Yes.

Parsimonious application of models is responsible use of public resources. In some cases, the calibration, maintenance, and operation of a conceptual model may not be economically justified. If the only forecast requirement is a seasonal volume, and extreme events are not problematic, statistical procedures may perform better than conceptual models and ESP. Figure 1 shows a comparison of regression and ESP based April-July RMS (root mean squared) forecast errors for the Blue River at Dillon, Colorado. In this case, regression provides better April-July forecasts but the management of the watershed requires shorter duration forecasts (i.e. weekly) that regression procedures cannot provide.

### SYSTEM DESCRIPTION

The CBRFC Statistical Water Supply (SWS) system is comprised of three subsystems:

1. Database Subsystem.
2. Calibration Subsystem.
3. Operational Subsystem.

#### Database Subsystem

The development of the database subsystem preceded the SWS system. The system primarily makes use of the Climate Database (CLIMATDB) portion of the CBRFC system of five linked relational databases structured under the RAPPORT database management system (dbms) on a PRIME minicomputer. The CLIMATDB holds station information, monthly hydrometeorological data, and all statistical model parameters and forecasts. In addition to the CLIMATDB, the system makes use of near real-time data posted to the Processed Database (PROCESSDB) from the Raw Database (RAWDB). See Figure 2.

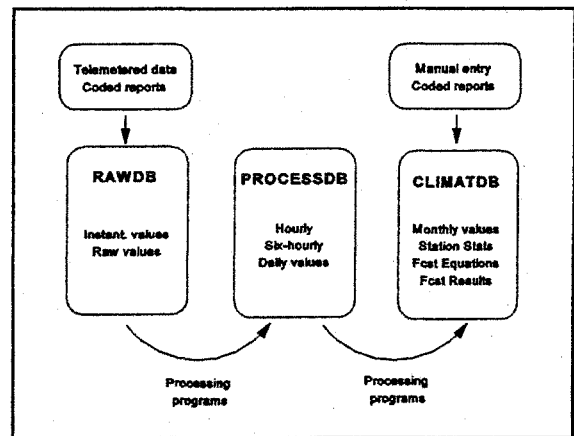


Figure 2. Database components and processing in support of SWS system.

The CLIMATDB contains a variety of data but is dominated by monthly streamflow volume, monthly diversion volume, end of month reservoir storage, monthly precipitation, and first of month snow water equivalent. Historical values were loaded from the most reliable source and new data are entered as they become available. Some stations have records that extend for over 100 years, however, the richest period of data begins in 1961.

Operationally, finalized values for stations are rarely available in time for inclusion in the statistical models. Therefore, provisional values are developed and stored in the CLIMATDB. Stations with automated telemetry are continuously collected in the RAWDB, processed into the PROCESSDB daily and moved to the CLIMATDB upon demand. For example, hourly instantaneous stream gage height might be processed into mean daily flow in the PROCESSDB and further processed to total monthly volume for preliminary storage in the CLIMATDB. Preliminary values are also available for many stations directly from the individuals or the agencies that collect them. These preliminary values are entered directly into CLIMATDB. When final values are available, the preliminary values are replaced. All data values in the CLIMATDB carry qualifiers that indicate if the value is observed, preliminary, estimated (low confidence), calculated (high confidence), or missing.

As will be described later, the operational system makes use of the PROCESSDB when exercising a first of month calibrated equation in a mid-month update.

It is important to note that water supply forecasts are usually made for the natural, unimpaired flow of the river basin at the forecast point, that is, the flow expected if water management activities were not performed upstream of the forecast point. To compute the natural streamflow, the observed streamflow is adjusted for all known and measured diversions and reservoir regulation upstream for which data are available. All data required to develop the natural flows are stored in the CLIMATDB and natural flows are programmatically computed based on the documented adjustments. Each fall, the CBRFC publishes a document that describes the natural flow adjustments made to each forecast point (Colorado Basin River Forecast Center, 1993).

### Calibration Subsystem

The calibration subsystem was designed to be easy to use, flexible, and powerful. The system is able to calibrate headwater basins, local basins, and routed points. Calibration consists of:

1. Identification of forecast points.
2. Screening the CLIMATDB for appropriate candidate predictor variables.
3. Development of calibration files with selected candidate predictor variables.
4. Calibration program runs.
5. Selection of primary and alternate (optional) equations.
6. Storage of selected equations and historical results in the CLIMATDB.

At this time, steps 1-3 and 6 are performed on the PRIME minicomputer while steps 4 and 5 are done on desktop PCs operating under the QNX operating system..

### Calibrational Approach

A sound and consistently applied calibration philosophy is critical to the development of a functional set of statistical forecast equations. In developing a calibrational philosophy, the user should consider the following issues:

#### *How often will forecasts be generated?*

Forecast frequency and timing dictate the type of equations that should be developed. If mid-month updates are required, the user must choose between developing explicit mid-month equations or executing first of month equations in a mid-month mode. If the later configuration is chosen, the system will perform best if daily incremental values are available for the monthly stations used in the equation calibrations.

#### *Are the best predictive data available when forecasts must be generated?*

Data availability must be considered in terms of when the forecast equations will be evaluated. If equations must be run on the first of the month, then only stations that are usually available on the first of the month should be considered. There is no value in including stations that will always be missing when forecasts must be generated. Some work suggests that the inclusion of future variables in a forecast equation may degrade the forecast performance (Garen, 1992).

If equation results are to be routed downstream, what base historical period is to be employed?

A river system of regression based forecast equations should exhibit a high level of connectivity. This connectivity requires that the historical calibration period overlap to the greatest extent possible. In some cases, headwater procedures with the lowest errors may not be optimal for the system if their period of record causes problems in routing procedures downstream.

Are missing years to be tolerated?

The calibration program does not deal with missing data in the best possible fashion. A specific combination of variables is evaluated using only the years in which all individual variables are non-missing. Thus, if missing values are included in the calibration input file, the specific years included will vary from one combination to another. This can lead to misleading results if an individual variable is missing in a year that was particularly difficult to forecast. In this case, the resulting CVSE for the combination of variables may be lower because a specific year was omitted rather than because a specific variable was included.

### Finding Candidate Variables

Once a forecast point and its' time series have been identified in the CLIMATDB, the developer screens the CLIMATDB for candidate variables. The objective of this process is to find a good set of candidate variables from which the forecast equation(s) can be developed. Prescreening is a crucial calibration step as the inclusion of junk variables slows the calibration program and may contaminate the results.

Specified program inputs include the runoff period (i.e. April through July), the correlation period (i.e. 1961 through 1990), and the geographic region to be considered. The candidate search program identifies all precipitation and snow measurement stations in the geographic region and computes single and contiguous multiple month correlations for precipitation stations and first of month correlations with snow water equivalent stations. Provided correlations include the number of observation pairs. Correlations with current and previous year streamflow periods are also computed to assess the potential benefit of a streamflow carryover variable. A sample of the output provided by the candidate search program is shown in Figure 3.

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RECCAND - GRFC NEXTREG CANDIDATE SEARCH PROGRAM

COLORADO - LAKE GRANBY, GRANBY, NR CO
LAT:401055 LONG:1055214 ELEV: 8280 DRAINAGE AREA: 12900
FORECAST PERIOD: APR-JUL
CORRELATION PERIOD: 1961-1990

Available: 4 5 6 7 8 9
1234567890123456789012345678901234567890
GBYC2 QCMPAZZ M0000000000000000000000000000000000

[0]bserved [m]issing [e]stimated [p]rovisional [c]alculated [ ]no record

LAT/LONG BOX:
-----4042-----
| 10610 |              | 10535 |
|-----|              |-----|
|-----4000-----|

Found: 4 Precip Stations
       7 SNOTEL Precip Sites
       11 Snow Courses
       7 SNOTEL Pillow Sites

PRECIPITATION SITES:
GDLC2 PPHRMZZ CO GRAND LAKE GSSW 4011 10552 8288 OCT NOV DEC JAN FEB MAR APR MAY
0.28(30) 0.48 0.69 0.74 0.74 0.79 0.80 0.85
NOV 0.45(30) 0.65 0.69 0.69 0.74 0.77 0.81
DEC 0.58(30) 0.56 0.62 0.65 0.74 0.74
JAN 0.22(30) 0.31 0.37 0.51 0.51
FEB 0.29(30) 0.33 0.45 0.45
MAR 0.16(30) 0.36 0.33
APR 0.41(30) 0.31
MAY 0.00(30)

SNOTEL PRECIPITATION SITES:
JWR22 PPHRMZZ CO JOE WRIGHT 4032 1055310120 OCT NOV DEC JAN FEB MAR APR MAY
0.38(11) 0.69 0.80 0.72 0.74 0.78 0.86 0.87
NOV 0.63(11) 0.75 0.59 0.62 0.65 0.79 0.82
DEC 0.59(11) 0.35 0.49 0.47 0.73 0.69
JAN -0.20(12) 0.04 0.08 0.54 0.46
FEB 0.27(12) 0.30 0.69 0.61
MAR 0.09(12) 0.76 0.52
APR 0.90(12) 0.64
MAY -0.16(12)

SNOW MEASUREMENT SITES:
CPAC2 SWIRRMZZ CO CAMERON PASS 4031 10553 10285 JAN FEB MAR APR MAY
0.80(17) 0.70(30) 0.70(30) 0.72(30) 0.73(30)

SNOTEL PILLOW SITES:
WLIC2 SWIRRMZZ CO WILLOW CREEK PASS 4021 10606 9540 JAN FEB MAR APR MAY
0.60(12) 0.66(30) 0.64(30) 0.69(30) 0.72(30)

CARRYOVER PERIOD CORRELATIONS:
PREVIOUS WATER YEAR PERIODS:
OCT-SEP 0.00 (29)
MAR-JUN -0.12 (29)
MAR-JUL -0.04 (29)
MAR-SEP 0.00 (29)
APR-JUN -0.12 (29)
APR-JUL -0.04 (29)
APR-SEP 0.00 (29)

CURRENT WATER YEAR PERIODS:
GBYC2 QCMPAZZ CO COLORADO - LAKE GRAN 4010 10552 8280 OCT NOV DEC JAN FEB MAR APR MAY
0.34(29) 0.41 0.48 0.51 0.53 0.55 0.45 0.59
NOV 0.48(29) 0.62 0.65 0.67 0.68 0.46 0.58
DEC 0.72(30) 0.72 0.74 0.74 0.42 0.55
JAN 0.53(30) 0.61 0.62 0.33 0.52
FEB 0.54(30) 0.54 0.27 0.51
MAR 0.42(30) 0.22 0.50
APR 0.17(30) 0.22 0.49
MAY 0.50(30)
```

Figure 3. Sample output from variable candidate search program (condensed).

By studying the candidate search results, the developer should be able to build a



Equation calibration runs are typically batched as they can take up to six hours to complete depending upon the number of variables, the number of years, and the speed of the computer. Once complete, programs exist to review the results in tabular and graphical form. The developer can review candidate equations to ensure they operate favorably under the required conditions.

### Equation Selection

Selection of equations requires the application of hydrologic judgment. Within an individual forecast equation the user must develop a balance between historical performance, as indicated by the CVSE, and the diversity and spatial distribution of station data. Good geographic coverage and variables that address more components of the seasonal water balance have a greater likelihood of performing well under unusual conditions. The equation with the lowest CVSE may only have one or two closely grouped stations and therefore may be unacceptable. If a set of monthly equations is to be developed, month to month consistency should be maintained to the highest level reasonable. Some shifting of stations will naturally occur from month to month but the overall structure of the equations should be consistent. If monthly equations are developed independently, the resulting set of monthly forecasts may be less consistent than they could be. Forecast adjustments from month to month should reflect a change in the watershed state rather than the use of a different forecast equation.

### Extracting Calibration Results

Parameters for selected equations are interactively stripped from the calibration run output and loaded into the CLIMATDB. When an equation is loaded into the CLIMATDB, it must be identified as primary or alternate. There can be one primary and up to twenty-six alternate equations for a specific forecast point, forecast time series, forecast period, and forecast date (e.g., Colorado at Kremmling, CO, adjusted streamflow, April through July, February 1). Primary equations normally represent the best balanced equation that meets all of the period of record requirements for routing downstream. Alternate equations are optionally developed to provide additional insight and perspective. Examples of alternate equations might include only snow data, only precipitation data, inclusion of a weather index, or exclusive use of telemetered stations. When a primary equation is loaded, the historical performance of the equation is stored for use in routed equations downstream. When an alternate equation is loaded, the user can overwrite an existing alternate equation or the system will assign a new alternate code. Figure 5 shows a primary and alternate equation as loaded into the CLIMATDB.

|                      |         |        |      |        |       |       |                      |         |        |      |       |       |       |
|----------------------|---------|--------|------|--------|-------|-------|----------------------|---------|--------|------|-------|-------|-------|
| GBYCZ/QCHPAZZ        | Apr-Jul | 61-90  | JSE: | 32.91  | SE:   | 30.85 | GBYCZ/QCHPAZZ        | Apr-Jul | 61-90  | JSE: | 36.20 | SE:   | 34.05 |
| COLORADO             | 0401P   | 100292 | JR2: | 0.73   | R2:   | 0.76  | COLORADO             | 0401s   | 100292 | JR2: | 0.67  | R2:   | 0.71  |
| LAKE GRANBY, GRANBY, |         | RKH    | n :  | 30     |       |       | LAKE GRANBY, GRANBY, |         | RKH    | n :  | 30    |       |       |
| COLORADO HEADWATERS  |         |        | #pc: | 1      | #var: | 6     | COLORADO HEADWATERS  |         |        | #pc: | 1     | #var: | 5     |
| GBYC2 QCHPAZZ        | Dec-Mar |        |      | 3.41   |       |       | NILC2 SWIRZZZ        | Apr     |        |      | 3.95  |       |       |
| GDLC2 FPHRZZZ        | Oct-Mar |        |      | 6.78   |       |       | GLAC2 SWIRZZZ        | Apr     |        |      | 3.92  |       |       |
| NILC2 SWIRZZZ        | Apr     |        |      | 3.44   |       |       | PKVC2 SWIRZZZ        | Apr     |        |      | 5.31  |       |       |
| GLAC2 SWIRZZZ        | Apr     |        |      | 3.54   |       |       | CPAC2 SWIRZZZ        | Apr     |        |      | 1.80  |       |       |
| PKVC2 SWIRZZZ        | Apr     |        |      | 4.90   |       |       | PHTC2 SWIRZZZ        | Apr     |        |      | 4.27  |       |       |
| CPAC2 SWIRZZZ        | Apr     |        |      | 1.71   |       |       | Intercept            |         |        |      | 4.45  |       |       |
| Intercept            |         |        |      | -27.95 |       |       |                      |         |        |      |       |       |       |

Figure 5. Sample primary and alternate forecast equations as loaded into the CLIMATDB.

### Routed Procedures

There are basically two types of equations: headwater and routed. Headwater equations are developed with predictor variables such as precipitation and snow water. Routed procedures are developed from the results of upstream forecast equations. When calibrated equations are loaded into the CLIMATDB, their historical results are also stored. Thus, when developing input data files for downstream routed forecast points, the system can access these data just as they would precipitation or snow water. It is important to develop the routed equations as a function of upstream forecasts rather than upstream observations. This configuration deals with procedural bias in upstream equations and allows the uncertainty associated with upstream forecasts to be properly translated downstream.

Although rather simple, the user has some choices to make in developing routed equations. The choices are associated with which upstream points will be included and whether or not individual weights will be utilized. From a statistical perspective, there is little reason to assign all routed elements the same relative weight. From a hydrologic perspective, this may make the most sense. In most cases, if the calibration program is allowed to assign

individual weights, the upstream point that is the most predictive will get the largest relative weight. Situations may occur where an upstream basin that contributes five percent of the downstream volume dominates a forecast equation. This may or may not be acceptable. If it is not, the user can combine the desired upstream forecasts into a single variable using the file building utility. Once equation coefficients have been estimated, they must be applied to each upstream forecast entity prior to loading into the CLIMATDB.

### Operational Subsystem

The operational system runs on the PRIME minicomputer and makes use of information stored in the CLIMATDB and PROCESSDB databases. When run, the operational program develops and stores up to five forecast quantities for each evaluated equation.

#### *Pure Computed*

This is the raw forecast equation result. For routed points, this reflects the use of purely raw equation results upstream.

#### *Computed with Coordinated*

This is only used for routed points and is the result of the routing equation when coordinated upstream forecasts are used as input.

#### *Coordinated*

This is the adjusted or agreed-to forecast for the point. These values are forced to adhere to the established rounding convention.

#### *NWS Preferred*

If coordination was not required, this is the forecast the NWS would have issued.

#### *Coordinating Agency Preferred*

This is similar to the NWS preferred, but is often the coordinating agencies initial or proposed forecast for the point.

It is anticipated that the collection of these five forecast quantities will provide insight into the benefits of judgmental forecast adjustment and coordination.

### Connectivity

When statistical water supply equations are developed, they are not explicitly identified as part of a major watershed forecast group. Individual equations stored in CLIMATDB are content independent of their application within a forecast river system. Normally, a river forecast system is a collection of headwater and routing procedures. Equations are evaluated and routed downstream in a specific order that creates consistency and continuity. Equation Group Driver Datasets (EGDDs) specify the order as well as what procedures are available to the forecast process. There is no limit to the number of EGDDs and a specific equation can be referenced in more than one EGDD.

### Operational Analysis

The operational water supply program can be run in either batch or interactive mode. The purpose of the batch program is to quickly evaluate all of the indicated equations within the specified EGDD. The output must be stored on disk and is normally printed for review. The interactive version is used to review and adjust forecasts as a result of additional hydrologic information, judgement, or coordination with another water management agency. When the operational program is invoked, the user must supply the desired EGDD file and the forecast date.

The notion of forecast date is very important because only forecasts with the same date can be routed downstream. First of month forecasts are always assigned the first of month date even if evaluated on the third or fourth day of the month. First of month forecasts access monthly data stored in the CLIMATDB.

If a date other than the first of a month is specified, the operation is considered 'mid-month'. Mid-month operations can either use explicitly calibrated mid-month equations or an equation designed for use on the first of a future month. Typically, one would use equations developed for the first of the next month, but this is not required. The user may select any future month but is required to characterize weather conditions between the specified forecast date and the date for which the equations were developed. Additionally, the user must characterize weather conditions between the first of the current month and the forecast date. The mid-month operation then uses the specified weather characterizations, daily observations from the PROCESSDB, and monthly observations and means from the CLIMATDB to estimate the data values required in the forecast equations. Mid-month operations are useful for updating forecast guidance and developing scenario forecasts. It should be noted that the uncertainty associated with this type of mid-month forecast is underestimated because some of the required data must be estimated. Scenario forecasts involve running a future month's set of equations (i.e. June 1) with various assumptions about future moisture input. Although interesting, special care must be taken when interpreting scenario forecasts since the uncertainties and probability distributions are not known.

Figure 6 shows the typical output from the batch operational program for a headwater and routed forecast point. Note that the output provides statistics on observed volumes, historical equation performance, a current equation evaluation, and a history of forecasts made in the current water year. The evaluated equation is broken down by individual data value so that the user can easily see which values are observed, provisional, or estimated and how each contributes to the total computed forecast. The forecast season history helps the user maintain month to month consistency and track procedure performance.

| GBYC2 QCMFAZZ Apr-Jul Volume         |         |                      |           |       |                        |      |       |   |       | EGLC2 QCMFAZZ Apr-Jul Volume         |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|--------------------------------------|---------|----------------------|-----------|-------|------------------------|------|-------|---|-------|--------------------------------------|---------|----------|---------|----------|-------------------------|-----|-----|--------------|--------------|---------------|-------------|--|--|--|--|--|--|--|--|--|--|
| Forecast Date: Mar 1 1994            |         |                      |           |       | Publ. Code: 0301P      |      |       |   |       | Forecast Date: Mar 1 1994            |         |          |         |          | Publ. Code: 0301P       |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Major Watershed: COLORADO HEADWATERS |         |                      |           |       | 61-90 Average: 214.0   |      |       |   |       | Major Watershed: COLORADO HEADWATERS |         |          |         |          | 61-90 Average: 1362.0   |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| River: COLORADO                      |         |                      |           |       | Median: 211.4          |      |       |   |       | River: COLORADO                      |         |          |         |          | Median: 1349.6          |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Location: LAKE GRANBY, GRANBY,       |         |                      |           |       | Std dev: 61.6          |      |       |   |       | Location: DOTSERO, NR                |         |          |         |          | Std dev: 478.2          |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Calibration MSE: 40.7                |         |                      |           |       | Hist Max (1984): 342.3 |      |       |   |       | Calibration MSE: 270.0               |         |          |         |          | Hist Max (1991): 3151.9 |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| R2: 0.58                             |         |                      |           |       | Min (1977): 117.2      |      |       |   |       | RS: 0.69                             |         |          |         |          | Min (1977): 563.8       |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| n: 30                                |         |                      |           |       |                        |      |       |   |       | n: 30                                |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| per: 61-90                           |         |                      |           |       |                        |      |       |   |       | per: 61-90                           |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| ID                                   | PC      | NAME                 | MTM       | COEF  | VALUE                  | SAVG | ICONT | Evaluation w/ pure upstream forecasts:        |       |                                      |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| GBYC2/QMFA                           |         | COLORADO - LAKE GRAN | Dec       | 5.66  | 3.79p                  | 103. | 10.   | ID  | PC    | NAME                                 | MTM     | COEF     | VALUE   | SAVG     | ICONT                   |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Jan       | 5.66  | 3.90p                  | 105. | 11.   | HSFC2/QMFA                                    |       | COLORADO - HOT SULPH                 | Apr-Jul | 1.03     | 390.67p | 101.     | 30.                     |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Feb       | 5.66  | 3.42p                  | 107. | 9.    | WSFC2/QMFA                                    |       | WILLIAMS FORK - WILL                 | Apr-Jul | 1.03     | 65.63p  | 98.      | 5.                      |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Oct       | 8.96  | 2.49p                  | 259. | 11.   | GRFC2/QMFA                                    |       | BLUE - GREEN MTN RES                 | Apr-Jul | 1.03     | 235.51p | 90.      | 18.                     |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Nov       | 8.96  | 0.75p                  | 80.  | 3.    | GPSC2/QMFA                                    |       | ENGLE - GYPSUM, BLO                  | Apr-Jul | 1.03     | 282.52p | 91.      | 21.                     |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Dec       | 8.96  | 0.57p                  | 63.  | 2.    | EGLC2/QMFL                                    |       | COLORADO - DOTSERO,                  | Apr-Jul | 1.03     | 341.08p | 99.      | 26.                     |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Jan       | 8.96  | 1.00p                  | 103. | 4.    | Intercept                                     |       |                                      |         |          |         |          |                         |     |     | -40.34       |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Feb       | 8.96  | 1.00p                  | 132. | 4.    | MP (kaf/%)                                    |       |                                      |         |          |         |          |                         |     |     | EP (%)       | RMAX (kaf/%) | RMIN (kaf/%)  |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Mar       | 5.79  | 8.60p                  | 112. | 24.   | Computed (pure)                               |       |                                      |         |          |         |          |                         |     |     | 1309.3 / 96. | 50.          | 1663.8 / 122. | 954.8 / 70. |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Mar       | 2.27  | 18.60p                 | 84.  | 20.   | Evaluation w/ coordinated upstream forecasts: |       |                                      |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Intercept | 18.31 |                        |      |       | ID  | PC    | NAME                                 | MTM     | COEF     | VALUE   | SAVG     | ICONT                   |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | HSFC2/QMFA                                    |       | COLORADO - HOT SULPH                 | Apr-Jul | 1.03     | 380.00c | 98.      | 29.                     |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | WSFC2/QMFA                                    |       | WILLIAMS FORK - WILL                 | Apr-Jul | 1.03     | 65.00c  | 97.      | 5.                      |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | GRFC2/QMFA                                    |       | BLUE - GREEN MTN RES                 | Apr-Jul | 1.03     | 250.00c | 95.      | 19.                     |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | GPSC2/QMFA                                    |       | ENGLE - GYPSUM, BLO                  | Apr-Jul | 1.03     | 290.00c | 94.      | 22.                     |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | EGLC2/QMFL                                    |       | COLORADO - DOTSERO,                  | Apr-Jul | 1.03     | 340.00c | 99.      | 26.                     |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | Intercept                                     |       |                                      |         |          |         |          |                         |     |     | -40.34       |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | MP (kaf/%)                                    |       |                                      |         |          |         |          |                         |     |     | EP (%)       | RMAX (kaf/%) | RMIN (kaf/%)  |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | Computed (w/coord.)                           |       |                                      |         |          |         |          |                         |     |     | 1319.1 / 97. | 49.          | 1673.6 / 123. | 964.6 / 71. |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | Coordinated                                   |       |                                      |         |          |         |          |                         |     |     | 1320.0 / 97. | 48.          | 1670.0 / 123. | 970.0 / 71. |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | NWS preferred                                 |       |                                      |         |          |         |          |                         |     |     | 1320.0 / 97. | 48.          |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       | Coord. agency pref.                           |       |                                      |         |          |         |          |                         |     |     | 1300.0 / 95. | 51.          |               |             |  |  |  |  |  |  |  |  |  |  |
| Forecast Season History (KAF/%):     |         |                      |           |       |                        |      |       |   |       | Forecast Season History (KAF/%):     |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      | Jan       | Feb   | Mar                    | Apr  | May   | Jun   |       |                                      |         | Jan      | Feb     | Mar      | Apr                     | May | Jun |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Comp                                 |         |                      |           |       |                        |      |       |   | Comp  |                                      |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Fcst                                 | 217/102 |                      | 221/103   |       | 225/105                |      |       |   | Fcst  | 1278/ 94                             |         | 1263/ 93 |         | 1309/ 96 |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Rmax                                 | 271/127 |                      | 273/128   |       | 279/130                |      |       |   | Rmax  | 1682/124                             |         | 1619/119 |         | 1664/122 |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Rmin                                 | 164/ 77 |                      | 169/ 79   |       | 172/ 80                |      |       |   | Rmin  | 874/ 64                              |         | 907/ 67  |         | 955/ 70  |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Coord                                |         |                      |           |       |                        |      |       |   | Coord |                                      |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Adj                                  | -2      |                      | -16       |       | -10                    |      |       |   | Diff  | -34                                  |         | 10       |         | 10       |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Fcst                                 | 215/100 |                      | 205/ 96   |       | 215/100                |      |       |   | Fcst  | 1244/ 91                             |         | 1272/ 93 |         | 1319/ 97 |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Rmax                                 | 270/126 |                      | 240/112   |       | 245/114                |      |       |   | Rmax  | 1649/121                             |         | 1628/120 |         | 1674/123 |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Rmin                                 | 160/ 75 |                      | 170/ 79   |       | 185/ 86                |      |       |   | Rmin  | 840/ 62                              |         | 917/ 67  |         | 965/ 71  |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| NWS                                  |         |                      |           |       |                        |      |       |   | Coord |                                      |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Fcst                                 | 205/ 96 |                      | 210/ 98   |       | 205/ 96                |      |       |   | Fcst  | 1250/ 92                             |         | 1270/ 93 |         | 1320/ 97 |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| C.A.                                 |         |                      |           |       |                        |      |       |   | Rmax  | 1650/121                             |         | 1630/120 |         | 1670/123 |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
| Fcst                                 | 215/100 |                      | 205/ 96   |       | 215/100                |      |       |   | Rmin  | 850/ 62                              |         | 910/ 67  |         | 970/ 71  |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       |   | NWS   |                                      |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       |   | Fcst  | 1250/ 92                             |         | 1260/ 93 |         | 1320/ 97 |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       |   | C.A.  |                                      |         |          |         |          |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |
|                                      |         |                      |           |       |                        |      |       |   | Fcst  | 1330/ 98                             |         | 1250/ 92 |         | 1300/ 95 |                         |     |     |              |              |               |             |  |  |  |  |  |  |  |  |  |  |

Figure 6. Sample of batch program output for basin (left) and routed (right) forecast points.

The interactive version of the operational program is primarily an adjustment and coordination utility. Based again on the forecast date and EGDD, the user interactively displays and enters forecast information. Values entered include the (1) coordinated most probable, reasonable maximum and minimum, (2) NWS preferred most probable forecast, and (3) coordinating agency preferred most probable forecast. Default values are provided where possible



to improve the ease of operation.

The EGDD defines the default order of processing but the user can move backward or jump to any point within the EGDD. Options exist to re-evaluate an equation, display full equation results, display and place the current forecast within the historical distribution, and review alternate equations. For routed points, the user can travel upstream and review those points, both routed and headwater, that contribute to the point currently under review. This upstream process can be repeated and allows the user to retrace the process back downstream to the original starting point. As such, a user could theoretically review all of the procedures in a major river basin by starting at the most downstream point.

An example of the information available during an interactive session is shown in Figure 7 for both a headwater and routed forecast point.

```

GBYC2/QCHPAZZ Apr-Jul Vol      61-90 Average: 214.0  Publ.code : 0301P
COLORADO                        Median : 211.4  Max (1984) : 342.3
LAKE GRANBY, GRANBY,          Std dev: 61.6  Min (1977) : 117.2

    Comp   Jan   Feb   Mar   Apr   May   Jun   Calib JSZ: 40.7
    Coord  215  205  215  215  215  215  R2: 0.58
    NWS    205  210  205  205  205  205  n: 30
    C.A.   215  205  215  215  215  215  period: 61-90

    Computed (pure)      MP (kaf/%)  EP (%)  RMAX (kaf/%)  RMIN (kaf/%)
    Coordinated          225.4 / 105.  50.     278.9 / 130.  171.9 / 80.
    NWS preferred        215.0 / 100.  60.     245.0 / 114.  185.0 / 86.
    Coord. agency pref. 205.0 / 96.   69.
    C.A. pref.           215.0 / 100.  60.

Adjust? (yes [no] display eval info jump back menu top quit): y
Coordinated MP [ 215.0]:
              RMAX [ 245.0]:
              RMIN [ 185.0]:
NWS pref. MP [ 205.0]:
C.A. pref. MP [ 215.0]:

ESL2C/QCHPAZZ Apr-Jul Vol      61-90 Average: 1362.0  Publ.code : 0301P
COLORADO                        Median : 1349.6  Max (1991) : 3151.9
DOTSERO, NR                      Std dev: 478.2  Min (1977) : 565.8

    Comp   Jan   Feb   Mar   Apr   May   Jun   Calib JSZ: 270.0
    Coord  1278  1263  1309  1244  1272  1319  R2: 0.69
    NWS    1250  1270  1320  1250  1260  1320  n: 30
    C.A.   1330  1250  1300  1300  1250  1300  period: 61-90

    Computed (pure)      MP (kaf/%)  EP (%)  RMAX (kaf/%)  RMIN (kaf/%)
    Coordinated (w/coord.) 1309.3 / 96.  50.     1663.8 / 122.  954.8 / 70.
    NWS preferred        1319.1 / 97.  49.     1673.6 / 123.  964.6 / 71.
    Coord. agency pref. 1320.0 / 97.  49.     1670.0 / 123.  970.0 / 71.
    C.A. pref.           1320.0 / 97.  48.
    C.A. pref.           1300.0 / 95.  51.

Adjust? (yes [no] display eval upstrm info jump back menu top quit): u

Upstream Adjustment for ESL2C/QCHPAZZ
COLORADO                        Computed: 1319.1 / 97% of avg
DOTSERO, NR                    Coordinated: 1320.0 / 97% of avg
                               difference: -0.9 / 0% of avg (-0.1% diff)

## ID/PC   Per   Location   Comp.Fcst   Coord.Fcst   EP
1 BTSC2/QCHPA Apr-Jul  BOT SULPHUR SPGS  390p / 101  380c / 98  55
2 WFOC2/QCHPA Apr-Jul  WILLIAMS FORK RES,  65t / 98  65c / 97  51
3 GBN2C/QCHPA Apr-Jul  GREEN MTN RES  245t / 94  250c / 95  45
4 GESC2/QCHPA Apr-Jul  GYPSUM, BLO  282p / 91  290c / 94  45
5 ESL2C/QCHPA Apr-Jul  DOTSERO, NR  341p / 99  340n / 99  50

Enter # or all ([r]eturn, jump, back, menu, top, quit)

```

Figure 7. Sample dialog for interactive version of operational program. The headwater point on the left shows the adjustment option. The routed point on the right shows upstream option.

### Operational Utilities

In addition to the above, the operational system provides for forecast dissemination and publication support as well as data requirements and data availability reports. Utilities exist to develop forecast summaries in the appropriate text format for (1) the "Water Supply Outlook for the Western United States", (2) "CBRFC Water Supply Outlook Reports", and (3) internal NWS products transmitted over AFOS (NWS communications system). Again, the content of these summaries is controlled by EGDDs and some EGDDs are maintained solely for publication and product summary purposes. Direct database generation of forecast information saves time and reduces errors.

The data requirements utility develops a complete summary of all data required by a group of equations for a month, a set of months or an entire forecast season. Again, the group of equations is defined by the EGDD. Data requirements are summarized by type and month. A data requirements list allows the RFC to properly align data collection efforts and advise cooperating agencies of their operational need for specific pieces of information. Figure 8 shows the type of information provided by the data requirements utility.

The data availability utility assess the current readiness of the CLIMATDB in terms of the data requirements of a group of equations on a specific date. Users will typically run this prior to making a forecast run. The utility provides a summary of what is available and what is still missing. This process helps to focus data collection efforts in anticipation of forecast runs.

| Station Name              | CHS5   | FEDSTEP | AGCY ID  | O | N | D | J | F | M | A | M | J | J | A | S |
|---------------------------|--------|---------|----------|---|---|---|---|---|---|---|---|---|---|---|---|
| BERTHOOD SUMMIT           | BTSC2  | PPHRMZZ | 05K145   | X | X | X | X | X | X | X | X | X | X | X | X |
| CASCADE                   | CSCC2  | PPHRMZZ | 07M055   | X | X | X |   |   |   |   |   |   |   |   |   |
| LAKE CONE                 | LWCC2  | PPHRMZZ | 08H075   | X | X | X |   |   |   |   |   |   |   |   |   |
| ASPEN 1 SW                | ASPC2  | PPHRMZZ | 05-0372  | X | X | X | X | X | X | X | X | X | X | X | X |
| BRECKENRIDGE              | BRCC2  | PPHRMZZ | 05-0909  | X | X | X |   |   |   |   |   |   |   |   |   |
| COLLBRN                   | CBNC2  | PPHRMZZ | 05-1741  | X | X | X |   |   |   |   |   |   |   |   |   |
| COLORADO - LAKE GRANBY, G | GBYC2  | QCHPAZZ | 09018500 | X | X | X | X | X | X | X |   |   |   |   |   |
| COLORADO - DOTSERO, NR    | EGL2C  | QCHLZZ  | 09070500 | X | X |   |   |   |   |   |   |   |   |   |   |
| EAST - ALMONT             | ALECC2 | QCHRZZ  | 09112500 | X | X |   |   |   |   |   |   |   |   |   |   |
| DOLORES - DOLORES         | DOLC2  | QCHRZZ  | 09166500 | X | X | X |   |   |   |   |   |   |   |   |   |
| ARENOW                    | AROC2  | SWIRMZZ | 05R065   |   |   |   |   |   | X | X | X | X |   |   |   |
| BRUNLEY                   | BRMC2  | SWIRMZZ | 06R405   |   |   |   |   |   | X | X | X | X |   |   |   |
| BERTHOOD SUMMIT           | BTSC2  | SWIRMZZ | 05K145   | X | X | X | X | X | X | X | X | X |   |   |   |
| BUTTE                     | BUTC2  | SWIRMZZ | 06L115   | X | X | X |   |   |   |   |   |   |   |   |   |
| BLUE RIVER                | BLIC2  | SWIRZ22 | 06K21    |   |   |   |   |   | X | X | X |   |   |   |   |
| COCHETOPA PASS            | CHPC2  | SWIRZ22 | 06L06    |   |   |   |   |   | X | X | X |   |   |   |   |
| CAMERON PASS              | CPAC2  | SWIRZ22 | 05J01    |   |   |   |   |   | X | X | X |   |   |   |   |
| GRAND LAKE                | GLAC2  | SWIRZ22 | 05J15    |   |   |   |   |   | X | X | X |   |   |   |   |

Figure 8. Sample output from data requirements utility.

## SYSTEM IMPLEMENTATION AND RESULTS

After reviewing the issues described under "Calibrational Approach", the CBRFC developed the following guidelines for primary equation development. Alternate equations could be developed without restrictions of any kind.

1. Forecast equations would be developed monthly, January through June for the upper Colorado and Great Basin, and January through May in the lower Colorado.

Since monthly equations were developed, the use of future data was prohibited. Thus an equation developed for use on January 1 could not reference a February 1 snow water equivalent.

2. The base period of forecasts would be 1961-1990. This would allow for routing of forecast results all through the system.
3. Missing data values would not be permitted. If a value was missing and could not be reliably estimated, the station value would not be used.

Formal development of the Statistical Water Supply (SWS) system began in the spring of 1991. The SWS prototype system was completed in the fall of 1991 and calibrations were made for all water supply points in Arizona as well as the Gunnison Basin in the upper Colorado. The system worked well in water year 1992. All CBRFC water supply points were calibrated in the fall of 1992 and the SWS system assumed full operational status in water year 1993. Scratch calibration (as opposed to recalibration) of all CBRFC regression based water supply procedures is a significant task. The fact that this was accomplished within a period of three months attests to the simplicity, utility, and performance of the calibration system. Currently the system holds more than a thousand calibrated equations.

Although it is not entirely fair to do so, it is interesting to compare the error statistics associated with the old and new statistical water supply forecasting systems. The old system relied upon a single seasonal equation that incorporated lumped indices of fall, winter, and spring precipitation, snow water equivalent (usually April 1), and an antecedent soil moisture term indexed by a period of previous streamflow runoff for the same forecast point. Not all indices were not required, individual station weights could be applied with indices, standard multiple linear regression was utilized, and line segments could be used to overcome non-linearity.

Figures 9 and 10 show a comparison of the equation standard errors for a headwater and routed water supply forecast point in the upper Colorado. Similar results were experienced throughout the CBRFC forecast area (Colorado Basin and eastern Great Basin). Since these are forecast equations, the more appropriate comparative index would be the CVSE. Unfortunately, CVSEs are not available for the older set of equations. Note that the new system provided a significant reduction in the standard error which translates into a higher level of forecast confidence and a narrower distribution of forecast uncertainty.

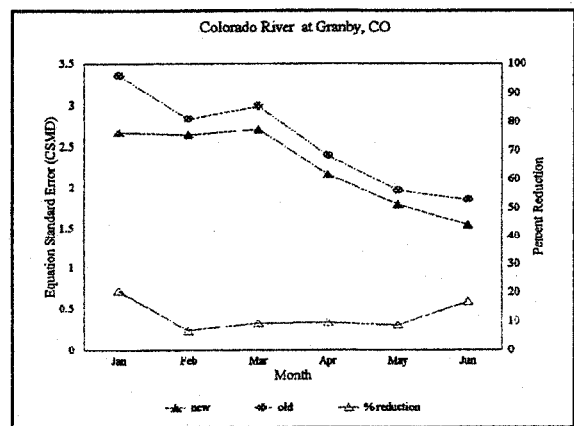


Figure 9. Comparison of old and new forecast equation standard error, Colorado River at Granby, CO.

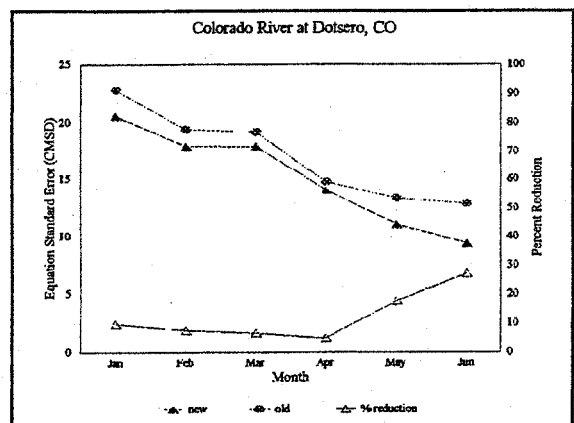


Figure 10. Comparison of old and new forecast equation standard error, Colorado River at Dotsero, CO.

## FUTURE SYSTEM ENHANCEMENTS / MODIFICATIONS

The primary planned system enhancement involves migration of the SWS system to a networked workstation environment. Database and computing resources available at the CBRFC mandated the multi-platform implementation of the prototype system. This configuration severely limits the extension of the SWS system to other NWS River Forecast Centers. Additionally, the calibration program does not have access to the database. This access will streamline the process and eliminate restrictions on the use of future data utilized in single seasonal equations. Porting efforts are currently underway and should be fully complete and operational prior to water year 1996. A limited scale version of the workstation-based system will be tested in water year 1995.

To date, the implementation of the SWS system at the CBRFC has not taken full advantage of the system flexibility. As stated previously, the system is capable of utilizing any information deemed hydrologically appropriate. Forecast errors originate from three sources: model error, data error, and weather error (uncertainty associated with future hydrometeorologic conditions). Of these, weather error is dominant, particularly at the beginning of the forecast season (Schaake and Peck, 1985). As such, the inclusion of long range weather forecasts and weather indices (Koch, 1989) in regression equations may offer significant benefits in terms of forecast accuracy and associated confidence.

## SUMMARY

Statistically based procedures have been, and will continue to be the primary tool for forecasting seasonal water supply volumes in the Western U.S. Over time, physically based models will assume a larger role, but in many cases, the effort and cost may not be justified. As such, the NWS has started the process of modernizing the techniques and tools required to provide the best possible guidance to its' user community. The SWS system takes advantage of relational databases, modern statistical techniques, and a systems approach that makes calibration and operation of the system straightforward and informative. Efforts are underway to extend the developed system to other NWS River Forecast Centers.

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